

Fixed sound source localization in reverberant environments using a multi-microphone set

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1 Introduction

The use of a series of microphones arranged in space (commonly called microphone arrays) is the subject of research in several areas. These include robotics, navigation, seismic monitoring, localization of speakers (teleconferencing), and hearing aids devices. Considering the fact that the distance from each microphone to the sound source is different, the sound emitted by the source will arrive at the observation points at a slightly different time. This lag time is used to deduce the direction of the sound source.

Generally, three classes of source localization algorithms are taken into account [1]. These methods can be classified according to the techniques used and based on the:

- i. Maximum output power steered beam former (SBF) [2,3].
- ii. High-resolution spectral estimation algorithm [4,5].
- iii. Time-delay estimation location technique [6,7,8].

In the first category, the source is localized by maximizing the output of a steerable beamformer. The approach combines delay-and-sum beamforming with statistical analysis to trace the position of the acoustic source. The method is effective when the source is emitting continuously but it may suffer when concurrent sound sources are present. In the second category, beamforming-based techniques are combined with high resolution spectral analysis. The third category is based on estimating the time difference (delay) between the incident wave and the pairs of microphones. These delays are used to determine the direction of the sound and are based generally on the auto-correlation [9, 10,11]. Knapp and Carter [12] proposed the generalized cross-correlation (GCC) method that was the most popular technique for TDOA (time delay of arrivals) estimation.

Other researchers [13, 14] proposed hybrid methods that combine the three previous categories.

In this work, we use a method based on time-delay estimation location technique. The aim of this study is the implementation of algorithms for locating a fixed sound source using a set of 4 microphones, arranged in a linear geometry and whose inter-microphone distances are known. This paper is organized as follows. In section 2, we introduce the Cross-power Spectrum Phase (CSP) [11] which does not require any a priori modeling of the noise statistics and is particularly suitable for wide band signals as speech. In section 3, we describe the experimental application setup. Section 4 reports the results of our study to illustrate algorithms performances in room acoustic environments where reverberation, noise and interference are commonly encountered. Conclusions close this paper in Section 5.

2 Modified Cross-power Spectral Phase (CSP)

Three categories of methods can be considered as an estimation of the incident wave where delays can be used to determine the direction of incidence [15]. These methods can be categorized by the techniques on which they are based, namely:

- Direction of incidence based on sound intensity;
- Time-delay estimation from cross-power spectral phase information;
- Time-delay estimation based on cross-correlation function analysis.

In the following, we use Time-delay estimation from cross-power spectral phase information.

Consider a source S and an array consisting of N receivers. For N=2, the original waveform s(t) emitted by a source S impinges on the microphones 0 and 1 after having been transformed by the convolution with the impulse responses between the source and the sensors:

$$x_i(t) = h_i(t) * s(t) + n_i(t)$$
 (1)

Where $x_i(t)$ is the microphone signal, $h_i(t)$ the impulse response and $n_i(t)$ the additive noise sequence.

An ideal propagation model assumes that the signal acquired by each sensor is a delayed (T_i) and attenuated (α_i) version of the original source signal. Mathematically, the received signals are expressed as:

$$x_i(t) = \alpha_i * s(t - T_i) \tag{2}$$

 α_i : scaling factor

 T_i : Propagation delay between the source sound S and the microphone i



Figure 1: Simple sound field of one source and two spatially separated microphones

The TDOA (Time Difference Of Arrival) is defined by $\tau = T_2 - T_1$, considering microphone 1 as a reference (Figure 1).

To estimate the delay between two microphones we usually consider the maximum of the cross-correlation $R_{12}(\tau)$ defined by:

$$R_{12}(\tau) = \int_{-\infty}^{\infty} x_1(t) * x_2(t-\tau) dt$$
(3)

This cross-correlation gives the similarity between the two signals $x_1(t)$ and $x_2(t)$. The cross-correlation function shows a maximum in τ corresponding to the direction of the incident wave. By considering the Fourier transforms $X_1(f)$ and $X_2(f)$ of the signals $x_1(t)$ and $x_2(t)$ respectively, the cross-correlation can be calculated by taking the inverse Fourier transform of the cross spectral power density $G_{12}(f)$:

$$R_{12}(\tau) = \int_{-\infty}^{\infty} G_{12}(f) e^{j2\pi f\tau} df$$
(4)

Where

$$G_{12}(f) = X_1(f) \cdot X_2(f)^*$$
(5)

This relationship is known as Wiener-Kinchine theorem.

The calculation of the Eq. (3) requires the integration of the signal on an infinitely long-time. However an estimate of the cross-correlation can be calculated on a finite time window of length T.

The choice of the observation period is an important parameter of the method. The optimal value is determined the experimental conditions (signal to noise ratio, reverberation) and CPU resources.

In the literature, a multiplicity of variants of generalized cross-correlation has been presented [11]. They basically introduce a weighting factor in order to take into account the source signal and noise statistics in a Maximum Likelihood scheme. The normalization factor is applied in order to preserve only the phase information Eq. (6):

$$G(f) = \frac{X_1(f) \cdot X_2(f)^*}{\|X_1(f)\| \cdot \|X_2(f)\|}$$
(6)

A version of this estimator was proposed by Rabinkin & al. [16] as the Modified Cross-Power Spectrum Phase (MCSP):

$$G(f) = \frac{X_1(f) \cdot X_2(f)^*}{(\|X_1(f)\| \cdot \|X_2(f)\|)^{\rho}} \qquad 0 < \rho < 1$$
(7)

Where ρ can be determined using characteristics of the noise and reverberations in a room. A good value of ρ can be estimated experimentally for different enclosures in normal rooms. If $\rho=0$, the algorithm becomes the unnormalized cross correlation while $\rho=1$ gives the cross power spectral density as shown in the Eq. (6).

The appropriate value of ρ can be determined experimentally according to the medium (ρ = 0.75 in a regular medium and $\rho = 0.8$ in a reverberant environment). This method is used to locate the source, but it is not robust in the presence of disturbance (probability of a false estimate for parts of the signal) [16]. Indeed, the presence of noise and reverberation can produce false peaks in the cross-correlation function. So, the analysis is performed by windows, reducing the instability of a peak with the hypothesis that the source does not change its position in a time interval. Both reverberation and noise, accounted for in the more realistic model in Eq. (1), contribute to increase the variance of the delay estimates and can produce spurious peaks in the CSP function. Consequently, a larger analysis window helps in reducing the instability of the correct peak, provided that the speaker does not change his/her position within the considered time interval. This observation suggests enhancing the estimation by averaging the CSP over multiple frames. In frequency domain this corresponds to an averaged cross-power spectrum:

$$G_{ph}(f) = \sum_{k=1}^{K} \frac{X_{1,k}(f) \cdot X_{2,k}(f)^{*}}{\left(\left\| X_{1,k}(f) \right\| \cdot \left\| X_{2,k}(f) \right\| \right)^{\rho}}$$
(8)

This method reduces the computational complexity and the effects of integration facilitate the estimate during a time interval corresponding to the analysis window [16].

After estimating the delay between the signals of the two microphones i and j, it is necessary to find the angle of the incident wave of each microphone based on the geometry of the arrangement of microphones. The far field assumptions consider the distance L between the source and the microphones much larger than the distance between two microphones. Hence, the incident waves can be assumed as parallel allowing simplified calculation [16].

A time delay, corresponding to the difference between the arrival of the acoustic wave front at microphone M_1 and microphone M_2 spaced by a distance d, is denoted as τ_{12} (Figure 12).



Figure 2: Acoustic wave front at microphones M₁ and M₂

Noting c the speed of sound in air, we can write:

$$\delta = d \cdot \sin(\theta) \tag{9}$$

$$\tau = \frac{\delta}{c} = \frac{d \cdot \sin(\theta)}{c} \tag{10}$$

We obtain a relation between the angle θ and the delay τ between the two signals. The knowledge of τ provides access to the angular position of the source relative to the axis of microphones.

3 Experimental section

In this work, we consider a source S and an array of 4 receivers. The experimental setup, which is outlined in Figure 13, shows the block diagram of the application. The implementation is performed in two parts. The first part represents the acquisition which uses a series of four identical omnidirectional microphones connected to their respective sound cards (4 USB sound cards). Recording files are used to estimate the direction of the angle of incidence using algorithms implemented in Matlab. After their acquisition to the desired sampling rate and after applying a high pass filter at 200 Hz to eliminate background noise, the signals are equalized.

The next step is the calculation of the FFT for each analysis window in order to evaluate the MCSP. First, we compute the product $X_i(f) \cdot X_j(f)^*$ for each frame of the signals considering microphones in pairs. Then, by dividing the result by the product ($||X_i(f)|| \cdot ||X_j(f)||$), we obtain the standard CSP, which allows keeping the phase information [16]. According to this reference, the latter product (denominator) is powered prior to $\rho= 0.8$ to eliminate background noise. The maximum of CSP corresponds to the time delay between the signals as observed in Figure 14. By averaging the CSP over multiple frames according to Eq. (8), we deduce the angle of incidence of the wave according to Eq. (10). The block diagram of the application steps is illustrated in Figure 15.



Figure 3: Block diagram of the implemented application



Figure 4: Time delay detection using MCSP algorithm



Figure 5: Angle estimation Algorithm using MCSP

4 **Results and Evaluation**

The objective of this study was the implementation of algorithms for locating a fixed sound source using a set of 4 microphones, arranged in a given geometry and whose inter-microphone distances are known.

The first problem was the simultaneous acquisition of multiple signals. A solution has been proposed by the use of multiple sound cards in helping us with Simulink (Matlab).

The second problem concerns highly reverberant environments that make particularly difficult estimation of the position of a reflecting barrier since a source signal can be seen as an independent source.

Our work concerns the detection of the direction of arrival of the incident wave (using general public microphones) and the duration of treatment in reverberant environments. To this end, the tests were carried out in a very reverberant room and with a significant background noise.

In this system, an array of four microphones classified into two pairs is arranged in linear; the distance of two adjacent microphones is d. They are placed in an empty room of 6m x 3m x 4m, without obstacles. The sampling frequency was Fe=44100Hz. In the series of tests conducted, we kept constant the distance d between microphones, while varying the angle of incidence of the sound source signal. These tests were repeated for different lengths of analysis windows.

Figure 6 (a, b and c) shows the results obtained for the estimating reception angles corresponding to different emitting angles $(30^\circ, 60^\circ \text{ and } 90^\circ)$, different intermicrophone distances (d=1, 2 and 3cm) and different lengths of treatment frames in seconds (0.0232 0.2322 1.1610 1.8576).

It was noticed that an effective estimation of the source was possible principally when the emitting source was facing the microphone array (source at 90°). In this case we can estimate the angle even for a relatively large time analysis widow: As illustrated in figure 6 (a) for d=1cm, good angle detection is obtained for durations of analysis windows between 24ms and 2s. In the case of d=2cm the good angle detection is obtained for a periodic analysis window comprised between 24ms and 200 ms. This period was between 24ms and 1.25s for d=3cm as shown in figure 6(c). Indeed, concerning the source placed at 30° and 60°, we can notice that good angle detection was obtained for a relatively short time analysis window (24ms to 250 ms) comparing to those obtained with 90° (24ms to 2s).

According to these results, we can roughly assume that good detections using this configuration correspond to time analysis window comprised between 24ms to 250 ms. The results are in agreement with the theory. In other words, highly reverberant environments make estimating the position of a reflecting barrier particularly difficult, since a source signal can be seen as independent and the treatment must be done before arrival of the reverberation wave.



Figure 6: Estimation of different incident angles corresponding to emitting angles of 30° , 60° and 90° and different distances between microphones (d=1cm, 2cm and 3cm) as function of time.

5 Conclusion

Theoretically we know that in an open space, the signal is reflected by any obstacle, such as walls, and it reaches the sensor by traversing a direct path (a straight line between the source and the sensor). Most applications that fall within are quite reverberant, as the signal received by a sensor is the sum of the direct path and the reflected signals through walls and other obstacles.

The highly reverberant environments make estimating the position of a reflecting barrier particularly difficult, since a source signal can be seen as independent and the treatment must be done before arrival of the reverberation wave.

The present study confirms this result. Thus for a time analysis window comprised between 24ms to 250 ms, there are good detections of incidence angles are obtained and we can see that the distance d = 1cm between the microphone gives better results.

The results obtained here use rather poor quality microphones and an acquisition system which is very simple. However, future work should be undertaken with an acquisition card from National Instruments NI PCI 4472 and microphones of better quality.

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